

# Semilattices of Groups in a Given Variety and Rectangular Bands

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In a recent scientific paper, Monzo characterized semilattices of rectangular bands and groups of exponent 2 as the semigroups that satisfy the following conditions:  $x = x^3$  and  $xyx \in \{xy^2x, y^2x^2y\}$ . In a subsequent paper, these semigroups were characterized by the following conditions:  $x = x^3$  and  $xy \in \{(xy)^2, yx\}$ . This characterization contains band's idempotency ( $xy = (xy)^2$ ) and the commutativity of groups of exponent 2 ( $xy = yx$ ), and hence is much more natural. But the key feature of this characterization is that it prompts the conjecture that semilattices of rectangular bands and groups satisfying the identity  $xy = v$  might be characterized by  $xy \in \{(xy)^2, v\}$ . The aim of this research was to prove this conjecture in fact holds for the special case of words  $v$  in which  $x$  and  $y$  appear the same number of times, the first letter is  $y$  and the last is  $x$ . As a very particular case of this general theorem we get the result that semilattices of rectangular bands and commutative groups are characterized by  $xy \in \{(xy)^2, yx\}$ .