Period-3 Point of Generalized Tent Mapping: Orbit Type and Stability Analysis

Shuai, Yi (School: Huayang High School)

Li-Yorke theorem shows for a continuous self-mapping in interval, if it has a period-3 point, it will have period-n point with any positive integer n. Therefore, period-3 point is worth exploring. This article studies a generalized tent mapping by using the continuity of mapping, cobweb plot and other methods. Vertex of this mapping is (a,b), left endpoint is (0,s) and right point is (1,c), while $0 < a < 1, 0 < b \le 1, 0 \le c < 1, 0 \le s < 1$. For such one-dimensional nonlinear mapping, this article shows the number of period-3 points and period-3 orbits when parameter space is four-dimensional. Besides, this article provides orbit type and stability analysis of period-3 orbit and predict the final direction of points on[0,1] under n iterations.