## **Gauss Circle Primes**

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Given a circle of radius r centered at the origin, the Gauss Circle Problem concerns counting the number of lattice points C(r) within this circle. It is known that as r grows large, the number of lattice points approaches pi  $r^2$ , that is, the area of the circle. This project seeks to study how often C(r) will return a prime number of lattice points for r less than or equal to n. We call a value of C(r) which is a prime number a Gauss Circle Prime. The researcher wrote a Java program to find the number of Gauss Circle Primes within a specified range of r. The Prime Number Theorem predicts that the number of primes less than or equal to n, called the prime number function p(n), is asymptotic to p(n) we find that for n less than or equal to p(n) and thus, (3) p(n) of Gauss Circle Primes for r less than or equal to n is also of order p(n) p(n) p(n) and thus, (3) p(n) p(n) gives a sharper approximation to p(n) than the Prime Number Theorem. We include a heuristic argument that for all integers n the Gauss Circle Primes can be approximated by a constant times p(n) p(n). The experimental data implies this constant is 1.

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