Analogues of the Robin-Lagarias Criteria for the Riemann Hypothesis

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Robin's criterion states that the Riemann hypothesis is equivalent to sigma(n) < $\exp(\text{gamma})$ n log log n for all integers n > 5040, where sigma(n) is the sum of divisors of n and gamma is the Euler-Mascheroni constant. We prove that the Riemann hypothesis is equivalent to the statement sigma(n) < $0.5\exp(\text{gamma})$ n log log n for all odd numbers n > $(3^4)(5^3)(7^2)(11)...(67)$. Lagarias's criterion for the Riemann hypothesis states that the Riemann hypothesis is equivalent to sigma(n) < H(n) + $\exp(H(n))\log(H(n))$ for all integers n > 1, where H(n) is the nth harmonic number. We establish an analogue to Lagarias's criterion for the Riemann hypothesis by creating a new harmonic series H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sigma(n) < H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sigma(n) < H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sigma(n) < H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sigma(n) < H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sigma(n) < H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sigma(n) < H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sigma(n) < H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sigma(n) < H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sigma(n) < H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sigma(n) < H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sigma(n) < H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sigma(n) < H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sigma(n) < H(n) = 2H(n) - H(2n) and demonstrating that the Riemann hypothesis is equivalent to sig